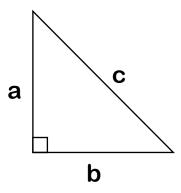
Right Angle Trigonometry

Trigonometry is the study of triangles in mathematics. We study angles and relationships with other angles and sides in a triangle.

In physics and engineering, we use this branch of math to help us calculate forces in structures, velocity of speeding objects, acceleration of rockets, and so much more!

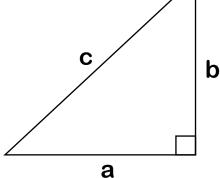
Parts of a Right Triangle



Sides "a" and "b" are <u>legs</u>. They form a right angle at their intersection.

Side "c" is the <u>hypotenuse</u>. This side is always opposite of the right angle.

The hypotenuse is always the longest side.

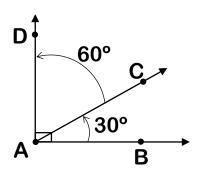


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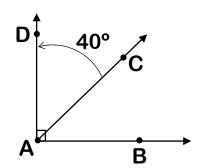
Types of **Angles**

Complementary angles always sum to 90°.

∠ DAC and ∠ CAB are complementary.

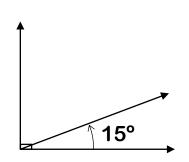


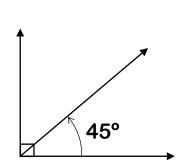
Find the missing angle:

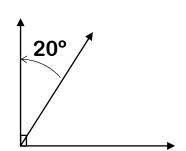


$$90^{\circ} - 40^{\circ} = 50^{\circ}$$

$$\angle$$
 CAB = 50°





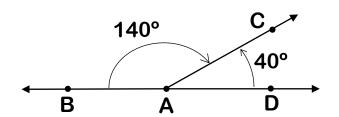


_____0

Supplementary angles always sum to 180°.

$$\angle$$
 BAC = 140° \angle CAD = 40°

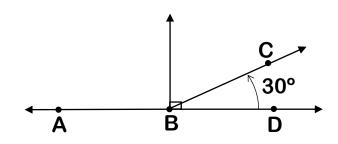
$$\angle$$
 CAD = 40°



$$\triangle DAB = \triangle BAC + \triangle CAD$$

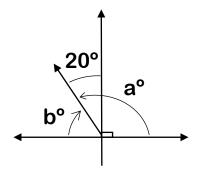
$$\triangle$$
 DAB = 140 + 40°
= 180°

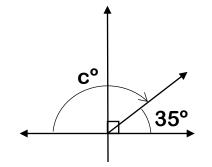
Find the missing angle:

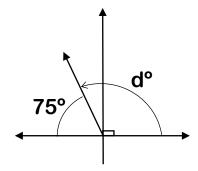


$$180^{\circ} - 30^{\circ} = 150^{\circ}$$

$$\triangle$$
 ABC = 150°



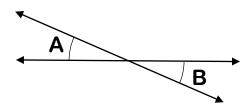




$$b^{\circ} = {}^{\circ}$$

$$\mathbf{c}^{\circ} = \mathbf{c}^{\circ}$$

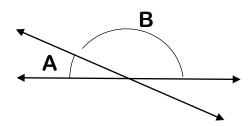
Angle Pairs



Vertical angles are opposite angles formed by intersecting lines.

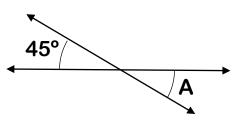
$$\triangle A = \triangle B$$

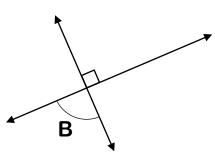
Adjacent angles are two angles that have a common side and vertex.

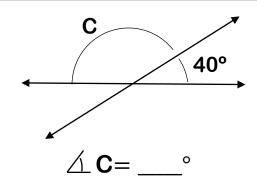


$$\triangle A + \triangle B = 180^{\circ}$$

Find the missing angle:





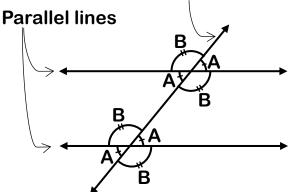




Parallel Lines & Transversals

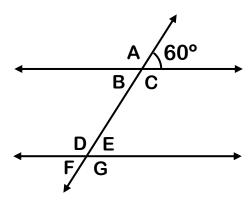
These parallel lines are intersected (cut) by a transversal, forming 8 different angles.

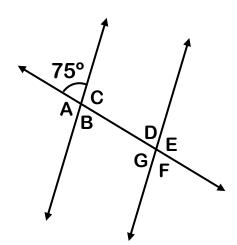
Transversal



- \triangle B are all congruent.
- \triangle A is supplementary to $\triangle B$.

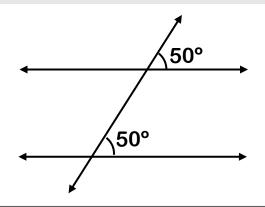
Label all 8 angles:

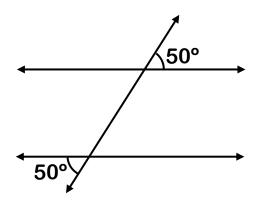




Types of Angle Pairs

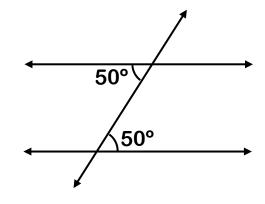
Corresponding angles are in the same relative position and are all congruent.

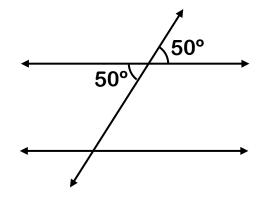




Alternating exterior angles are outside the parallel lines and on opposite sides of the transversal.

Alternating interior angles are on the inside of the parallel lines and on opposite sides of the transversals.

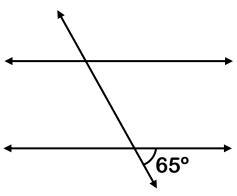


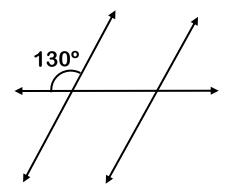


Vertical angles are formed by intersecting lines and are on opposite sides.

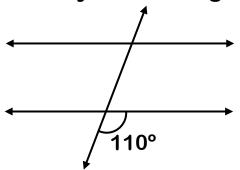
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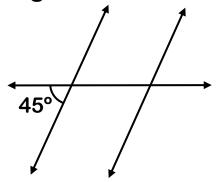
Find all missing angles and label the transversal:



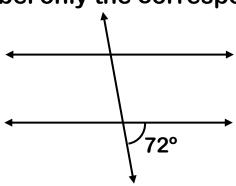


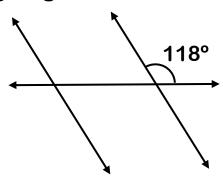
Label only alternating interior angles:



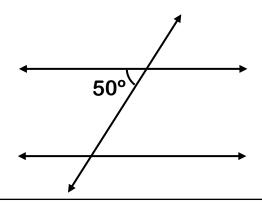


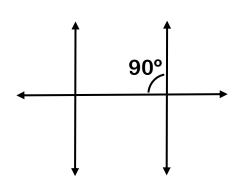
Label only the corresponding angle:





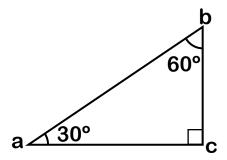
Label only the alternating exterior angles:





Angles of a Triangle

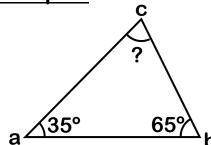
The sum of all angles in a triangle is always 180°.



$$\triangle a + \triangle b + \triangle c = 180^{\circ}$$

$$30^{\circ} + 60^{\circ} + 90^{\circ} = 180^{\circ}$$

Example:



$$\triangle a + \triangle b + \triangle c = 180^{\circ}$$

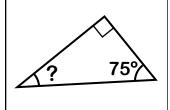
$$4.35^{\circ} + 4.65^{\circ} + 4.c = 180^{\circ}$$

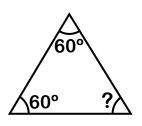
$$\angle 100^{\circ} + \angle \mathbf{c} = 180^{\circ}$$

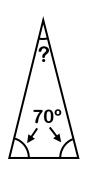
$$\triangle c = 180^{\circ} - 100^{\circ}$$

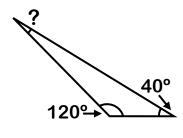
$$\sqrt{\mathbf{c}} = 80^{\circ}$$

Find the missing angles:



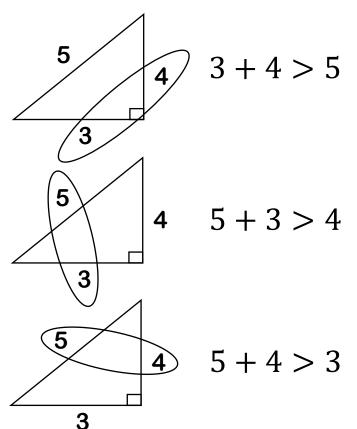




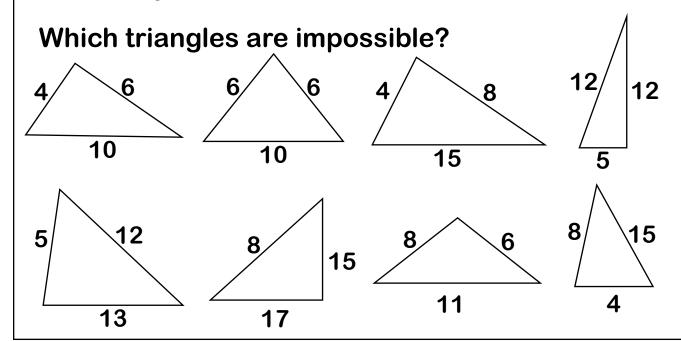


Triangle Constraints

The sum of any two sides <u>must</u> be greater than the third.

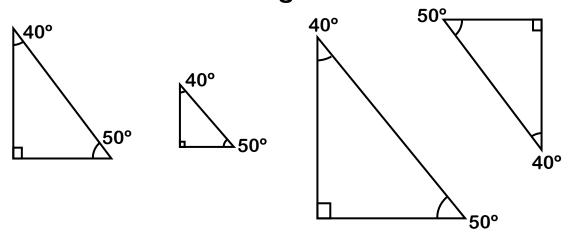


One Unique
Triangle:
3 side
lengths that
meet these
requirements
will always
make 1
unique
triangle



Triangle Constraints

More than one triangle can be made from knowing only the angles of a triangle. These are called <u>similar triangles</u>, or congruent triangles



In order to make a congruent triangle unique, you must constrain (specify) at least one side length.

How many triangles are possible?

a) side lengths: 4, 2, 6

d) \$\\ 30\circ\$, 60\circ\$, 90\circ\$

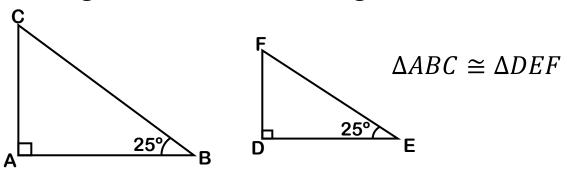
b) side lengths: 5, 12, 13 e) \$\times 45^\circ\$, 55^\circ\$, 95^\circ\$

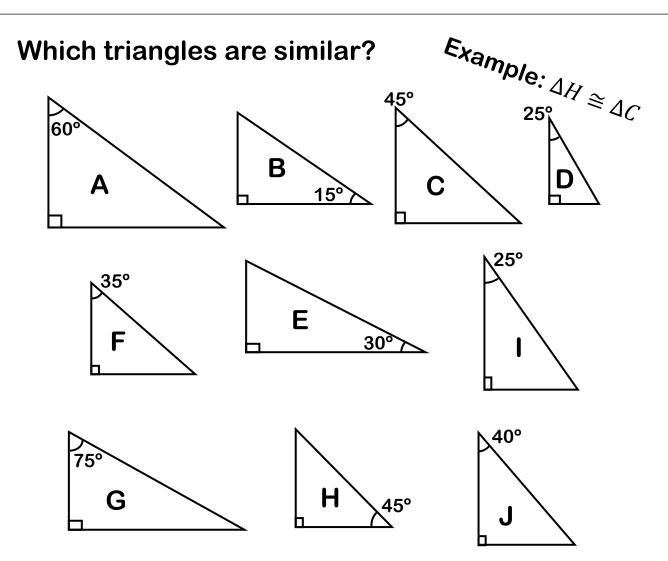
c) side lengths: 3, 4, 5

f) ∡ 30°, 45°, and

hypotenuse=7

Similar triangles: If two triangles have two pairs of corresponding angles that are congruent, then the triangles are similar

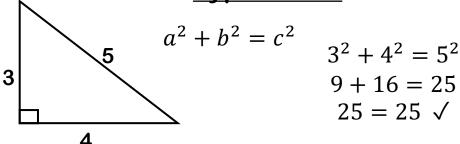


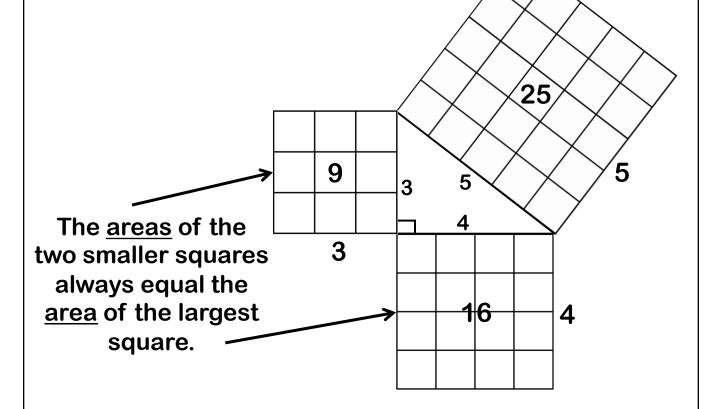


Pythagorean Theorem

only for right ∆'s

In a right triangle, the sum of the squares
of the shorter sides equals the squares
of the hypotenuse.





This means that is you check to see if $a^2 + b^2 = c^2$ and it's true, then you know it's a right triangle.

Pythagorean Converse

Which triangles are right triangles?

side lengths:

5, 12, 13
$$5^2 + 12^2 = 13^2$$

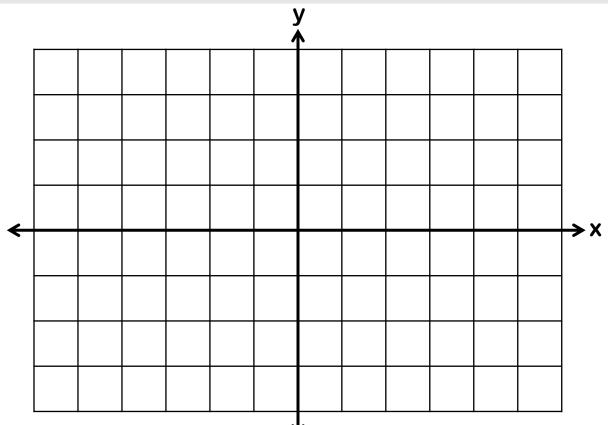
$$3^2 + 4^2 = 7^2$$

8, 15, 17
$$8^2 + 15^2 = 17^2$$

Using a ruler,

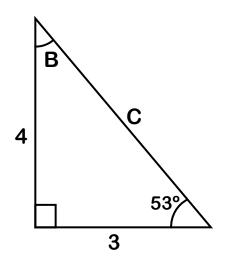
Draw one of the right triangles from above using either cm or mm on your ruler (whichever is best).





- 1 Plot the points: A = (4, -3) B = (-3, 2)C = (-3, -3)
- (2) Connect the dots to form a triangle
- 3 Use your protractor to measure 4A = _____ ach angle: 4B = _____
- 4 Use your ruler to measure the hypotenuse
- Compare the measured hypotenuse with using the Pythagorean Theorem to find the diagonal distance between points A and B

Finding sides and angles of Right triangles:



Use your understanding of angles and the Pythagorean theorem to find all the missing sides and angles for each triangle

$$c^{2} = 4^{2} + 3^{2}$$

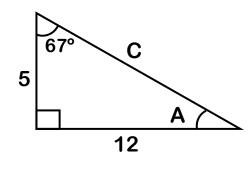
$$c^{2} = 16 + 9$$

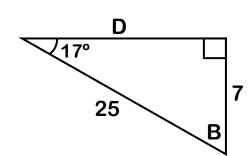
$$c^{2} = 25$$

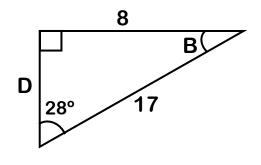
$$\sqrt{c^{2}} = \sqrt{25}$$

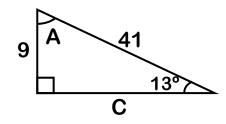
$$c = 5$$

Now you try:









Trigonometry Ratios

Sine (sin) is the ratio of

Cosine (cos) is the ratio of

opposite side hypotenuse

adjacent side hypotenuse hypotenuse

opposite

adjacent

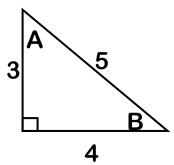
*The hypotenuse is always across from the right angle.

*The opposite and adjacent sides depend on the angle

adjacent

opposite

Example:



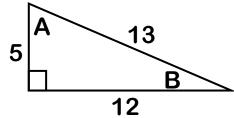
$$\sin(A) = \frac{4}{5} \qquad \cos(A) = \frac{3}{5}$$

$$=\frac{1}{5}$$
 $\cos(A) =$

$$\sin(B) = \frac{3}{5}$$

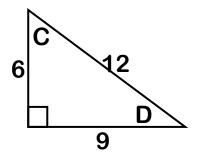
$$\sin(B) = \frac{3}{5} \qquad \cos(B) = \frac{4}{5}$$

Now you try:



$$\sin(A) = -\cos(A) = -$$

$$\sin(B) = - \cos(B) = -$$



$$sin(C) = - cos(C) = -$$

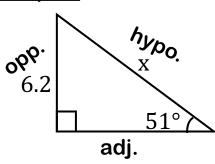
$$sin(D) = - cos(D) = -$$

Using ratios to find the missing side/angle

Steps to find a missing side

- 1. Label the sides (opposite, adjacent, hypotenuse)
- 2. Identify which trig ratio to use (sin, cos)
- 3. Set up an equation
- 4. Solve (using a calculator)

Example:



$$\sin(\theta) = \frac{opposite}{hypotenuse}$$

$$\sin(51) = \frac{6.2}{x}$$

$$51^{\circ}$$

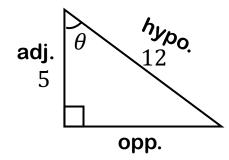
$$6.2 \div \sin(51) = x$$

$$x = 8$$

Steps to find a missing angle

- 1. Label the sides (opposite, adjacent, hypotenuse)
- 2. Identify which trig ratio to use (sin, cos)
- 3. Set up an equation
- 4. Use the inverse trig ratio (sin⁻¹, cos⁻¹) to solve *Theta (θ) is the variable for an angle

Example:



$$cos(\theta) = \frac{adjacent}{hypotenuse}$$

$$cos(\theta) = \frac{5}{12}$$
$$cos^{-1} \left(\frac{5}{12}\right) = x$$
$$x = 65^{\circ}$$

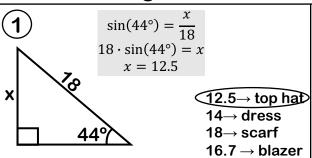
Sines-Math Lib

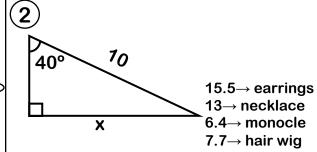
Wearing a (1)_____ and (2)____, the (3)____ was

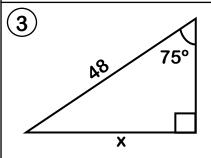
(4)_____ the (5)____ and (6)____on top

of a (7)_____ to impress (8)_____.

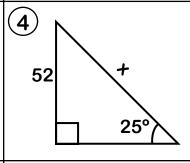
Find the missing sides to fill in the blanks (use a calculator):



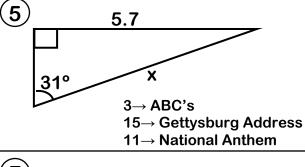


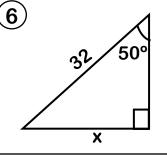


18.5→ mouse 12.4→ cat 50→ lizard 46.4→ dog

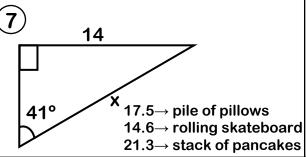


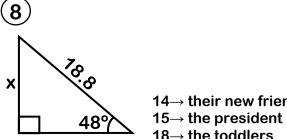
22→ yelling 123→ singing 47→ whispering 50.7→ smelling





24.5→ dancing 20→ jumping 18→ twirling 41.7→ skating





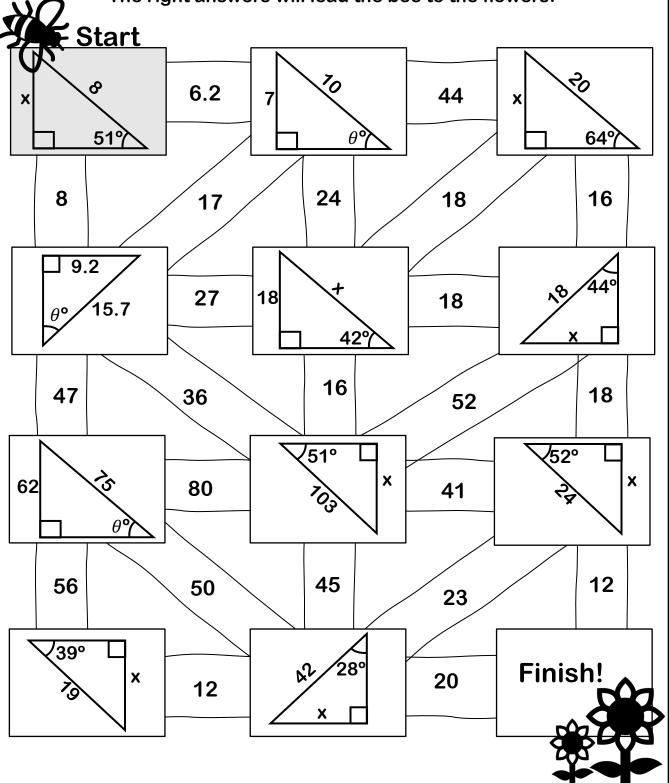
14→ their new friends

18→ the toddlers

Sines-Maze

Determine the missing length of the right triangle described in each box and follow the answer to the next box.

The right answers will lead the bee to the flowers!



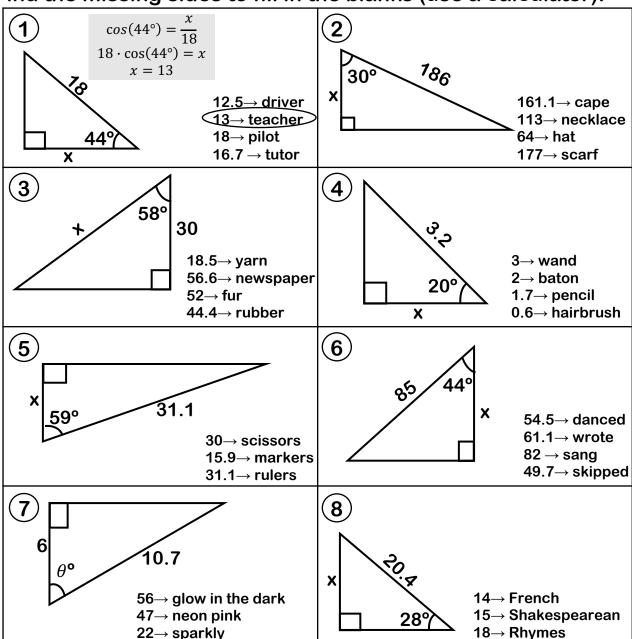
Cosines- Math Lib

The (1)_____, wearing a (2)____ made of (3)____ and

holding a (4)_____ made of (5)_____, (6)____ using

(7)_____ paint while speaking in (8)_____.

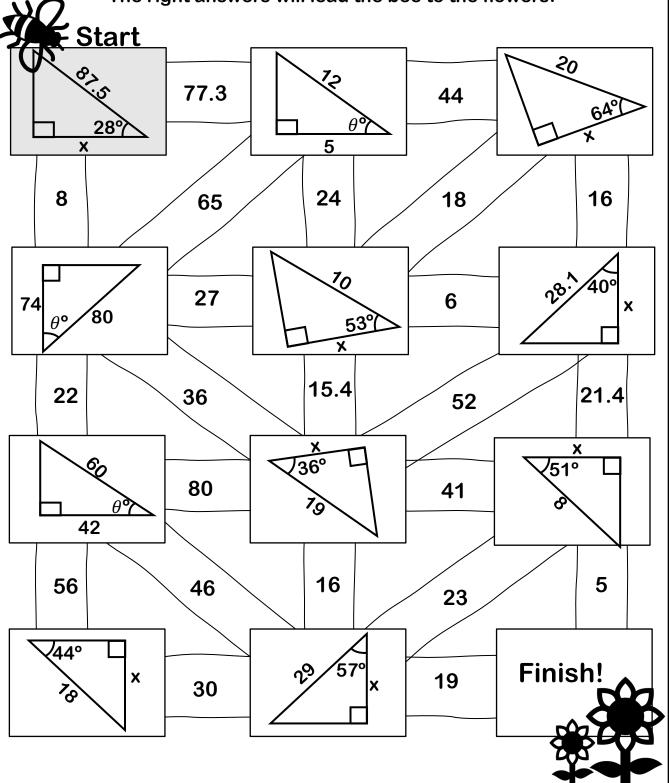
Find the missing sides to fill in the blanks (use a calculator):



Cosines-Maze

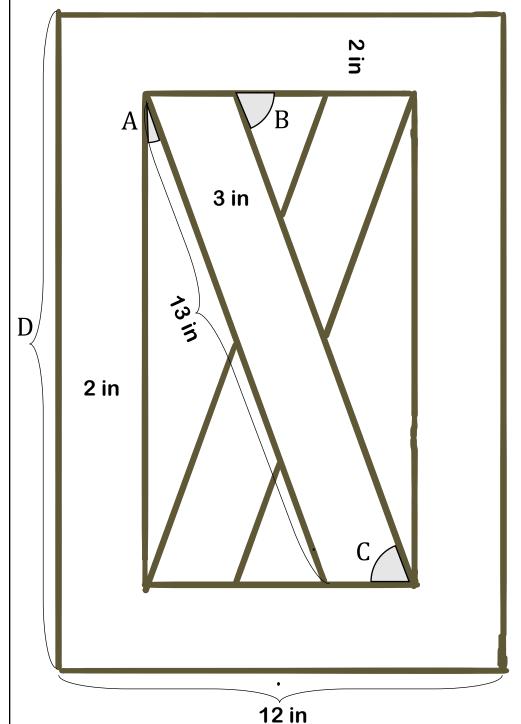
Determine the missing length of the right triangle described in each box and follow the answer to the next box.

The right answers will lead the bee to the flowers!



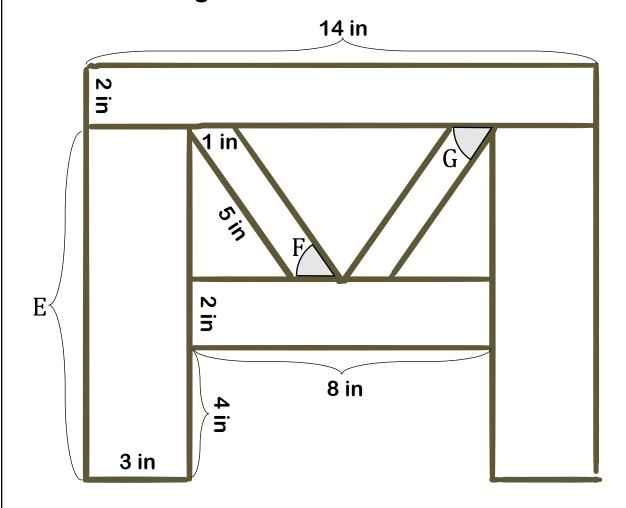
Real World Applications for Right Triangles Practice Test

Find the missing measurements of this door:



Real World Applications for Right Triangles Practice Test

Find the missing measurements of this table:



Real World Applications for Right Triangles Practice Test

Find the missing measurements of this cabin:

